

# Package ‘glmGamPoi’

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**Type** Package

**Title** Fit a Gamma-Poisson Generalized Linear Model

**Version** 1.8.0

**Description** Fit linear models to overdispersed count data.

The package can estimate the overdispersion and fit repeated models for matrix input. It is designed to handle large input datasets as they typically occur in single cell RNA-seq experiments.

**License** GPL-3

**Encoding** UTF-8

**SystemRequirements** C++11

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as.list.glmGamPoi	<i>Convert glmGamPoi object to a list</i>
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### Description

Convert glmGamPoi object to a list

### Usage

```
## S3 method for class 'glmGamPoi'
as.list(x, ...)
```

### Arguments

x	an object with class glmGamPoi
...	not used

### Value

The method returns a list with the following elements:

**Beta** a matrix with dimensions `nrow(data) x n_coefficients` where `n_coefficients` is based on the `design` argument. It contains the estimated coefficients for each gene.

**overdispersions** a vector with length `nrow(data)`. The overdispersion parameter for each gene. It describes how much more the counts vary than one would expect according to the Poisson model.

`Mu` a matrix with the same dimensions as `dim(data)`. If the calculation happened on disk, than `Mu` is a `HDF5Matrix`. It contains the estimated mean value for each gene and sample.

`size_factors` a vector with length `ncol(data)`. The size factors are the inferred correction factors for different sizes of each sample. They are also sometimes called the exposure factor.

`model_matrix` a matrix with dimensions `ncol(data) × n_coefficients`. It is build based on the `design` argument.

---

 glm\_gp

*Fit a Gamma-Poisson Generalized Linear Model*


---

## Description

This function provides a simple to use interface to fit Gamma-Poisson generalized linear models. It works equally well for small scale (a single model) and large scale data (e.g. thousands of rows and columns, potentially stored on disk). The function automatically determines the appropriate size factors for each sample and efficiently finds the best overdispersion parameter for each gene.

## Usage

```
glm_gp(
  data,
  design = ~1,
  col_data = NULL,
  reference_level = NULL,
  offset = 0,
  size_factors = c("normed_sum", "deconvolution", "poscounts"),
  overdispersion = TRUE,
  overdispersion_shrinkage = TRUE,
  ridge_penalty = 0,
  do_cox_reid_adjustment = TRUE,
  subsample = FALSE,
  on_disk = NULL,
  verbose = FALSE
)
```

## Arguments

<code>data</code>	any matrix-like object (e.g. <code>matrix</code> , <code>DelayedArray</code> , <code>HDF5Matrix</code> ) or anything that can be cast to a <code>SummarizedExperiment</code> (e.g. <code>MSnSet</code> , <code>eSet</code> etc.) with one column per sample and row per gene.
<code>design</code>	a specification of the experimental design used to fit the Gamma-Poisson GLM. It can be a <code>model.matrix()</code> with one row for each sample and one column for each coefficient. Alternatively, <code>design</code> can be a formula. The entries in the formula can refer to global objects, columns in the <code>col_data</code> parameter, or the <code>colData(data)</code> of <code>data</code> if it is a <code>SummarizedExperiment</code> .

The third option is that `design` is a vector where each element specifies to which condition a sample belongs.

Default: `design = ~ 1`, which means that all samples are treated as if they belong to the same condition. Note that this is the fastest option.

<code>col_data</code>	a dataframe with one row for each sample in data. Default: NULL.
<code>reference_level</code>	a single string that specifies which level is used as reference when the model matrix is created. The reference level becomes the intercept and all other coefficients are calculated with respect to the <code>reference_level</code> . Default: NULL.
<code>offset</code>	Constant offset in the model in addition to $\log(\text{size\_factors})$ . It can either be a single number, a vector of length <code>ncol(data)</code> or a matrix with the same dimensions as <code>dim(data)</code> . Note that if data is a <a href="#">DelayedArray</a> or <a href="#">HDF5Matrix</a> , <code>offset</code> must be as well. Default: $\emptyset$ .
<code>size_factors</code>	<p>in large scale experiments, each sample is typically of different size (for example different sequencing depths). A size factor is an internal mechanism of GLMs to correct for this effect.</p> <p><code>size_factors</code> is either a numeric vector with positive entries that has the same lengths as columns in the data that specifies the size factors that are used. Or it can be a string that species the method that is used to estimate the size factors (one of <code>c("normed_sum", "deconvolution", "poscounts")</code>). Note that "normed_sum" and "poscounts" are fairly simple methods and can lead to sub-optimal results. For the best performance, I recommend to use <code>size_factors = "deconvolution"</code> which calls <code>scran::calculateSumFactors()</code>. However, you need to separately install the <code>scran</code> package from Bioconductor for this method to work. Also note that <code>size_factors = 1</code> and <code>size_factors = FALSE</code> are equivalent. If only a single gene is given, no size factor is estimated (ie. <code>size_factors = 1</code>). Default: "normed_sum".</p>
<code>overdispersion</code>	<p>the simplest count model is the Poisson model. However, the Poisson model assumes that <math>\text{variance} = \text{mean}</math>. For many applications this is too rigid and the Gamma-Poisson allows a more flexible mean-variance relation (<math>\text{variance} = \text{mean} + \text{mean}^2 * \text{overdispersion}</math>).</p> <p><code>overdispersion</code> can either be</p> <ul style="list-style-type: none"> <li>• a single boolean that indicates if an overdispersion is estimated for each gene.</li> <li>• a numeric vector of length <code>nrow(data)</code> fixing the overdispersion to those values.</li> <li>• the string "global" to indicate that one dispersion is fit across all genes.</li> </ul> <p>Note that <code>overdispersion = 0</code> and <code>overdispersion = FALSE</code> are equivalent and both reduce the Gamma-Poisson to the classical Poisson model. Default: TRUE.</p>
<code>overdispersion_shrinkage</code>	the overdispersion can be difficult to estimate with few replicates. To improve the overdispersion estimates, we can share information across genes and shrink each individual overdispersion estimate towards a global overdispersion estimate. Empirical studies show however that the overdispersion varies based on the mean expression level (lower expression level => higher dispersion). If

	overdispersion_shrinkage = TRUE, a median trend of dispersion and expression level is fit and used to estimate the variances of a quasi Gamma Poisson model (Lund et al. 2012). Default: TRUE.
ridge_penalty	<p>to avoid overfitting, we can penalize fits with large coefficient estimates. Instead of directly minimizing the deviance per gene (<math>Sumdev(y_i, X_i b)</math>), we will minimize <math>Sumdev(y_i, X_i b) + N * Sum(penalty_p * b_p)^2</math>.</p> <p>ridge_penalty can be</p> <ul style="list-style-type: none"> <li>• a scalar in which case all parameters except the intercept are penalized.</li> <li>• a vector which has to have the same length as columns in the model matrix</li> <li>• a matrix with the same number of columns as columns in the model matrix. This gives maximum flexibility for expert users and allows for full Tikhonov regularization.</li> </ul> <p>Default: ridge_penalty = 0, which is internally replaced with a small positive number for numerical stability.</p>
do_cox_reid_adjustment	<p>the classical maximum likelihood estimator of the overdispersion is biased towards small values. McCarthy <i>et al.</i> (2012) showed that it is preferable to optimize the Cox-Reid adjusted profile likelihood.</p> <p>do_cox_reid_adjustment can be either be TRUE or FALSE to indicate if the adjustment is added during the optimization of the overdispersion parameter. Default: TRUE.</p>
subsample	<p>the estimation of the overdispersion is the slowest step when fitting a Gamma-Poisson GLM. For datasets with many samples, the estimation can be considerably sped up without losing much precision by fitting the overdispersion only on a random subset of the samples. Default: FALSE which means that the data is not subsampled. If set to TRUE, at most 1,000 samples are considered. Otherwise the parameter just specifies the number of samples that are considered for each gene to estimate the overdispersion.</p>
on_disk	<p>a boolean that indicates if the dataset is loaded into memory or if it is kept on disk to reduce the memory usage. Processing in memory can be significantly faster than on disk. Default: NULL which means that the data is only processed in memory if data is an in-memory data structure.</p>
verbose	<p>a boolean that indicates if information about the individual steps are printed while fitting the GLM. Default: FALSE.</p>

## Details

The method follows the following steps:

1. The size factors are estimated.  
 If size\_factors = "normed\_sum", the column-sum for each cell is calculated and the resulting size factors are normalized so that their geometric mean is 1. If size\_factors = "poscounts", a slightly adapted version of the procedure proposed by Anders and Huber (2010) in equation (5) is used. To handle the large number of zeros the geometric means are calculated for  $Y + 0.5$  and ignored during the calculation of the median. Columns with all zeros get a default size factor of 0.001. If size\_factors = "deconvolution", the method `scran::calculateSumFactors()` is called.

2. The dispersion estimates are initialized based on the moments of each row of  $Y$ .
3. The coefficients of the model are estimated.  
If all samples belong to the same condition (i.e. `design = ~ 1`), the betas are estimated using a quick Newton-Raphson algorithm. This is similar to the behavior of edgeR. For more complex designs, the general Fisher-scoring algorithm is used. Here, the code is based on a fork of the internal function `fitBeta()` from DESeq2. It does however contain some modification to make the fit more robust and faster.
4. The mean for each gene and sample is calculate.  
Note that this step can be very IO intensive if data is or contains a `DelayedArray`.
5. The overdispersion is estimated.  
The classical method for estimating the overdispersion for each gene is to maximize the Gamma-Poisson log-likelihood by iterating over each count and summing the the corresponding log-likelihood. It is however, much more efficient for genes with many small counts to work on the contingency table of the counts. Originally, this approach had already been used by Anscombe (1950). In this package, I have implemented an extension of their method that can handle general offsets.  
See also `overdispersion_mle()`.
6. The beta coefficients are estimated once more with the updated overdispersion estimates
7. The mean for each gene and sample is calculated again.

This method can handle not just in memory data, but also data stored on disk. This is essential for large scale datasets with thousands of samples, as they sometimes encountered in modern single-cell RNA-seq analysis. `glmGamPoi` relies on the `DelayedArray` and `beachmat` package to efficiently implement the access to the on-disk data.

## Value

The method returns a list with the following elements:

- `Beta` a matrix with dimensions `nrow(data) x n_coefficients` where `n_coefficients` is based on the `design` argument. It contains the estimated coefficients for each gene.
- `overdispersions` a vector with length `nrow(data)`. The overdispersion parameter for each gene. It describes how much more the counts vary than one would expect according to the Poisson model.
- `overdispersion_shrinkage_list` a list with additional information from the quasi-likelihood shrinkage. For details see `overdispersion_shrinkage()`.
- `deviances` a vector with the deviance of the fit for each row. The deviance is a measure how well the data is fit by the model. A smaller deviance means a better fit.
- `Mu` a matrix with the same dimensions as `dim(data)`. If the calculation happened on disk, than `Mu` is a `HDF5Matrix`. It contains the estimated mean value for each gene and sample.
- `size_factors` a vector with length `ncol(data)`. The size factors are the inferred correction factors for different sizes of each sample. They are also sometimes called the exposure factor.
- `Offset` a matrix with the same dimensions as `dim(data)`. If the calculation happened on disk, than `Offset` is a `HDF5Matrix`. It contains the `log(size_factors) + offset` from the function call.
- `data` a `SummarizedExperiment` that contains the input counts and the `col_data`

`model_matrix` a matrix with dimensions `ncol(data) × n_coefficients`. It is build based on the design argument.

`design_formula` the formula that used to fit the model, or NULL otherwise

`ridge_penalty` a vector with the specification of the ridge penalty.

## References

- McCarthy, D. J., Chen, Y., & Smyth, G. K. (2012). Differential expression analysis of multifactor RNA-Seq experiments with respect to biological variation. *Nucleic Acids Research*, 40(10), 4288–4297. <https://doi.org/10.1093/nar/gks042>.
- Anders Simon, & Huber Wolfgang. (2010). Differential expression analysis for sequence count data. *Genome Biology*. <https://doi.org/10.1016/j.jcf.2018.05.006>.
- Love, M. I., Huber, W., & Anders, S. (2014). Moderated estimation of fold change and dispersion for RNA-seq data with DESeq2. *Genome Biology*, 15(12), 550. <https://doi.org/10.1186/s13059-014-0550-8>.
- Robinson, M. D., McCarthy, D. J., & Smyth, G. K. (2009). edgeR: A Bioconductor package for differential expression analysis of digital gene expression data. *Bioinformatics*, 26(1), 139–140. <https://doi.org/10.1093/bioinformatics/btp616>.
- Lun ATL, Pagès H, Smith ML (2018). “beachmat: A Bioconductor C++ API for accessing high-throughput biological data from a variety of R matrix types.” *PLoS Comput. Biol.*, 14(5), e1006135. doi: [10.1371/journal.pcbi.1006135](https://doi.org/10.1371/journal.pcbi.1006135).
- Lund, S. P., Nettleton, D., McCarthy, D. J., & Smyth, G. K. (2012). Detecting differential expression in RNA-sequence data using quasi-likelihood with shrunken dispersion estimates. *Statistical Applications in Genetics and Molecular Biology*, 11(5). <https://doi.org/10.1515/1544-6115.1826>.
- Lun ATL, Bach K and Marioni JC (2016). Pooling across cells to normalize single-cell RNA sequencing data with many zero counts. *Genome Biol.* 17:75 <https://doi.org/10.1186/s13059-016-0947-7>

## See Also

`overdispersion_mle()` and `overdispersion_shrinkage()` for the internal functions that do the work. For differential expression analysis, see `test_de()`.

## Examples

```
set.seed(1)
# The simplest example
y <- rnbinom(n = 10, mu = 3, size = 1/2.4)
c(glm_gp(y, size_factors = FALSE))

# Fitting a whole matrix
model_matrix <- cbind(1, rnorm(5))
true_Beta <- cbind(rnorm(n = 30), rnorm(n = 30, mean = 3))
sf <- exp(rnorm(n = 5, mean = 0.7))
model_matrix
Y <- matrix(rnbinom(n = 30 * 5, mu = sf * exp(true_Beta %*% t(model_matrix)), size = 1/2.4),
           nrow = 30, ncol = 5)
```

```

fit <- glm_gp(Y, design = model_matrix, size_factors = sf, verbose = TRUE)
summary(fit)

# Fitting a model with covariates
data <- data.frame(fav_food = sample(c("apple", "banana", "cherry"), size = 50, replace = TRUE),
  city = sample(c("heidelberg", "paris", "new york"), size = 50, replace = TRUE),
  age = rnorm(n = 50, mean = 40, sd = 15))
Y <- matrix(rnbinom(n = 100 * 50, mu = 3, size = 1/3.1), nrow = 100, ncol = 50)
fit <- glm_gp(Y, design = ~ fav_food + city + age, col_data = data)
summary(fit)

# Specify 'ridge_penalty' to penalize extreme Beta coefficients
fit_reg <- glm_gp(Y, design = ~ fav_food + city + age, col_data = data, ridge_penalty = 1.5)
summary(fit_reg)

```

---

loc_median_fit	<i>Estimate local median fit</i>
----------------	----------------------------------

---

## Description

This function fits  $y$  based on  $x$  through a (weighted) median using the  $\text{npoints}/2$  neighborhood.

## Usage

```

loc_median_fit(
  x,
  y,
  fraction = 0.1,
  npoints = max(1, round(length(x) * fraction)),
  weighted = TRUE,
  ignore_zeros = FALSE
)

```

## Arguments

<code>x, y</code>	the $x$ and $y$ coordinates of the points.
<code>fraction, npoints</code>	the fraction / number of the points that are considered for each fit. <code>npoints</code> is the argument that is used in the end it is at least one. Default: <code>fraction = 0.1</code> and <code>npoints = length(x) * fraction</code> .
<code>weighted</code>	a boolean that indicates if a weighted median is calculated.
<code>ignore_zeros</code>	should the zeros be excluded from the fit

## Details

This function is low-level implementation detail and should usually not be called by the user.



**See Also**

locfit: a package dedicated to local regression.

**Examples**

```
x <- runif(n = 1000, max = 4)
y <- rpois(n = 1000, lambda = x * 10)

plot(x, y)
fit <- loc_median_fit(x, y, fraction = 0.1)
points(x, fit, col = "red")
```

---

overdispersion\_mle      *Estimate the Overdispersion for a Vector of Counts*

---

**Description**

Estimate the Overdispersion for a Vector of Counts

**Usage**

```
overdispersion_mle(
  y,
  mean,
  model_matrix = NULL,
  do_cox_reid_adjustment = !is.null(model_matrix),
  global_estimate = FALSE,
  subsample = FALSE,
  max_iter = 200,
  verbose = FALSE
)
```

**Arguments**

y	a numeric or integer vector or matrix with the counts for which the overdispersion is estimated
mean	a numeric vector of either length 1 or length(y) or if y is a matrix, a matrix with the same dimensions. Contains the predicted value for that sample. If missing: mean(y) / rowMeans(y)
model_matrix	a numeric matrix that specifies the experimental design. It can be produced using stats::model.matrix(). Default: NULL
do_cox_reid_adjustment	the classical maximum likelihood estimator of the overdispersion is biased towards small values. McCarthy <i>et al.</i> (2012) showed that it is preferable to optimize the Cox-Reid adjusted profile likelihood.

	do_cox_reid_adjustment can be either be TRUE or FALSE to indicate if the adjustment is added during the optimization of the overdispersion parameter. Default: TRUE if a model matrix is provided, otherwise FALSE
global_estimate	flag to decide if a single overdispersion for a whole matrix is calculated instead of one estimate per row. This parameter has no affect if y is a vector. Default: FALSE
subsample	the estimation of the overdispersion is the slowest step when fitting a Gamma-Poisson GLM. For datasets with many samples, the estimation can be considerably sped up without loosing much precision by fitting the overdispersion only on a random subset of the samples. Default: FALSE which means that the data is not subsampled. If set to TRUE, at most 1,000 samples are considered. Otherwise the parameter just specifies the number of samples that are considered for each gene to estimate the overdispersion.
max_iter	the maximum number of iterations for each gene
verbose	a boolean that indicates if information about the individual steps are printed while fitting the GLM. Default: FALSE.

## Details

The function is optimized to be fast on many small counts. To achieve this, the frequency table of the counts is calculated and used to avoid repetitive calculations. If there are probably many unique counts the optimization is skipped. Currently the heuristic is to skip if more than half of the counts are expected to be unique. The estimation is based on the largest observed count in y.

An earlier version of this package (< 1.1.1) used a separate set of functions for the case of many small counts based on a paper by Bandara et al. (2019). However, this didn't bring a sufficient performance increase and meant an additional maintenance burden.

## Value

The function returns a list with the following elements:

`estimate` the numerical estimate of the overdispersion.

`iterations` the number of iterations it took to calculate the result.

`message` additional information about the fitting process.

## See Also

[glm\\_gp\(\)](#)

## Examples

```
set.seed(1)
# true overdispersion = 2.4
y <- rnbino(n = 10, mu = 3, size = 1/2.4)
# estimate = 1.7
overdispersion_mle(y)
```

```

# true overdispersion = 0
y <- rpois(n = 10, lambda = 3)
# estimate = 0
overdispersion_mle(y)
# with different mu, overdispersion estimate changes
overdispersion_mle(y, mean = 15)
# Cox-Reid adjustment changes the result
overdispersion_mle(y, mean = 15, do_cox_reid_adjustment = FALSE)

# Many very small counts, true overdispersion = 50
y <- rnbinom(n = 1000, mu = 0.01, size = 1/50)
summary(y)
# estimate = 31
overdispersion_mle(y, do_cox_reid_adjustment = TRUE)

# Function can also handle matrix input
Y <- matrix(rnbinom(n = 10 * 3, mu = 4, size = 1/2.2), nrow = 10, ncol = 3)
Y
as.data.frame(overdispersion_mle(Y))

```

---

overdispersion\_shrinkage

*Shrink the overdispersion estimates*


---

### Description

Low-level function to shrink a set of overdispersion estimates following the quasi-likelihood and Empirical Bayesian framework.

### Usage

```

overdispersion_shrinkage(
  disp_est,
  gene_means,
  df,
  disp_trend = TRUE,
  ql_disp_trend = NULL,
  ...,
  verbose = FALSE
)

```

### Arguments

`disp_est`            vector of overdispersion estimates  
`gene_means`        vector of average gene expression values. Used to fit `disp_trend` if that is `NULL`.

<code>df</code>	degrees of freedom for estimating the Empirical Bayesian variance prior. Can be length 1 or same length as <code>disp_est</code> and <code>gene_means</code> .
<code>disp_trend</code>	vector with the dispersion trend. If NULL or TRUE the dispersion trend is fitted using a (weighted) local median fit. Default: TRUE.
<code>ql_disp_trend</code>	a logical to indicate if a second abundance trend using splines is fitted for the quasi-likelihood dispersions. Default: NULL which means that the extra fit is only done if enough observations are present.
<code>...</code>	additional parameters for the <code>loc_median_fit()</code> function
<code>verbose</code>	a boolean that indicates if information about the individual steps are printed while fitting the GLM. Default: FALSE.

### Details

The function goes through the following steps

1. Fit trend between overdispersion MLE's and the average gene expression. Per default it uses the `loc_median_fit()` function.
2. Convert the overdispersion MLE's to quasi-likelihood dispersion estimates by fixing the trended dispersion as the "true" dispersion value:  $disp_{ql} = (1 + mu * disp_{mle}) / (1 + mu * disp_{trend})$
3. Shrink the quasi-likelihood dispersion estimates using Empirical Bayesian variance shrinkage (see Smyth 2004).

### Value

the function returns a list with the following elements

**dispersion\_trend** the dispersion trend provided by `disp_trend` or the local median fit.

**ql\_disp\_estimate** the quasi-likelihood dispersion estimates based on the dispersion trend, `disp_est`, and `gene_means`

**ql\_disp\_trend** the `ql_disp_estimate` still might show a trend with respect to `gene_means`. If `ql_disp_trend = TRUE` a spline is used to remove this secondary trend. If `ql_disp_trend = FALSE` it corresponds directly to the dispersion prior

**ql\_disp\_shrunken** the shrunken quasi-likelihood dispersion estimates. They are shrunken towards `ql_disp_trend`.

**ql\_df0** the degrees of freedom of the empirical Bayesian shrinkage. They correspond to spread of the `ql_disp_estimate`'s

### References

- Lund, S. P., Nettleton, D., McCarthy, D. J., & Smyth, G. K. (2012). Detecting differential expression in RNA-sequence data using quasi-likelihood with shrunken dispersion estimates. *Statistical Applications in Genetics and Molecular Biology*, 11(5). <https://doi.org/10.1515/1544-6115.1826>.
- Smyth, G. K. (2004). Linear models and empirical bayes methods for assessing differential expression in microarray experiments. *Statistical Applications in Genetics and Molecular Biology*, 3(1). <https://doi.org/10.2202/1544-6115.1027>

**See Also**

```
limma::squeezeVar()
```

**Examples**

```
Y <- matrix(rnbinom(n = 300 * 4, mu = 6, size = 1/4.2), nrow = 30, ncol = 4)
disps <- sapply(seq_len(nrow(Y)), function(idx){
  overdispersion_mle(Y[idx, ])$estimate
})
shrink_list <- overdispersion_shrinkage(disps, rowMeans(Y), df = ncol(Y) - 1,
                                       disp_trend = FALSE, ql_disp_trend = FALSE)

plot(rowMeans(Y), shrink_list$ql_disp_estimate)
lines(sort(rowMeans(Y)), shrink_list$ql_disp_trend[order(rowMeans(Y))], col = "red")
points(rowMeans(Y), shrink_list$ql_disp_shrunken, col = "blue", pch = 16, cex = 0.5)
```

---

predict.glmGamPoi      *Predict 'link' or 'response' values for Gamma-Poisson GLMs*

---

**Description**

Predict  $\mu$  (i.e., `type = "response"`) or  $\log(\mu)$  (i.e., `type = "link"`) from a `'glmGamPoi'` fit (created by `glm_gp(...)`) with the corresponding estimate of the standard error. If `newdata` is `NULL`,  $\mu$  is returned for the original input data.

**Usage**

```
## S3 method for class 'glmGamPoi'
predict(
  object,
  newdata = NULL,
  type = c("link", "response"),
  se.fit = FALSE,
  offset = mean(object$Offset),
  on_disk = NULL,
  verbose = FALSE,
  ...
)
```

**Arguments**

<code>object</code>	a <code>glmGamPoi</code> fit object (produced by <code>glm_gp()</code> ).
<code>newdata</code>	a specification of the new data for which the expression for each gene is predicted. <code>newdata</code> should be a

	<p><b>data.frame</b> if the original fit was specified with a formula, provide a <code>data.frame</code> with one column for each variable in the formula. For example, if <code>glm_gp(se, design = ~ age + batch + treatment)</code>, then the <code>data.frame</code> needs a <code>age</code>, <code>batch</code>, and <code>treatment</code> column that contain the same data types as the original fit.</p> <p><b>vector</b> if the original fit was specified using a vector, you need to again provide a vector with the same format.</p> <p><b>matrix</b> if <code>newdata</code> is a matrix, it is applied directly as <code>Mu &lt;- exp(object\$Beta %*% t(newdata) + object\$offset_matrix)</code>. So make sure, that it is constructed correctly.</p> <p><b>NULL</b> if <code>newdata</code> is <code>NULL</code>, the predicted values for the original input data are returned.</p>
<code>type</code>	either 'link' or 'response'. The default is 'link', which returns the predicted values before the link function ( <code>exp()</code> ) is applied. Thus, the values can be positive and negative numbers. However, often the predicted values are easier to interpret <b>after</b> the link function is applied (i.e., <code>type = "response"</code> ), because then the values are on the same scale as the original counts.
<code>se.fit</code>	boolean that indicates if in addition to the mean the standard error of the mean is returned.
<code>offset</code>	count models (in particular for sequencing experiments) usually have a sample specific size factor ( <code>offset = log(size factor)</code> ). It defines how big we expect the predicted results are. If <code>newdata</code> is <code>NULL</code> , the <code>offset</code> is ignored, because the <code>predict()</code> returns a result based on the pre-calculated <code>object\$Mu</code> . If <code>newdata</code> is not <code>NULL</code> , by default the <code>offset</code> is <code>mean(object\$Offset)</code> , which puts the in the same size as the average sample.
<code>on_disk</code>	a boolean that indicates if the results are <code>HDF5Matrix</code> 's from the <code>HDF5Array</code> package. If <code>newdata</code> is <code>NULL</code> , <code>on_disk</code> is ignored. Otherwise, if <code>on_disk = NULL</code> , the result is calculated on disk depending if <code>offset</code> is stored on disk.
<code>verbose</code>	a boolean that indicates if information about the individual steps are printed while predicting. Default: <code>FALSE</code> .
<code>...</code>	currently ignored.

### Details

For `se.fit = TRUE`, the function sticks very close to the behavior of `stats::predict.glm()` for fits from `MASS::glm.nb()`.

### Value

If `se.fit == FALSE`, a matrix with dimensions `nrow(object$data) x nrow(newdata)`.

If `se.fit == TRUE`, a list with three entries

**fit** the predicted values as a matrix with dimensions `nrow(object$data) x nrow(newdata)`. This is what would be returned if `se.fit == FALSE`.

**se.fit** the associated standard errors for each fit. Also a matrix with dimensions `nrow(object$data) x nrow(newdata)`.

**residual.scale** Currently fixed to 1. In the future, this might become the values from `object$overdispersion_shrinkage_`

**See Also**

[stats::predict.lm\(\)](#) and [stats::predict.glm\(\)](#)

**Examples**

```

set.seed(1)
# The simplest example
y <- rbinom(n = 10, mu = 3, size = 1/2.4)
fit <- glm_gp(y, size_factors = FALSE)
predict(fit, type = "response")
predict(fit, type = "link", se.fit = TRUE)

# Fitting a whole matrix
model_matrix <- cbind(1, rnorm(5))
true_Beta <- cbind(rnorm(n = 30), rnorm(n = 30, mean = 3))
sf <- exp(rnorm(n = 5, mean = 0.7))
model_matrix
Y <- matrix(rbinom(n = 30 * 5, mu = sf * exp(true_Beta %*% t(model_matrix)), size = 1/2.4),
           nrow = 30, ncol = 5)
fit <- glm_gp(Y, design = model_matrix, size_factors = sf, verbose = TRUE)

head(predict(fit, type = "response"))
pred <- predict(fit, type = "link", se.fit = TRUE, verbose = TRUE)
head(pred$fit)
head(pred$se.fit)

# Fitting a model with covariates
data <- data.frame(fav_food = sample(c("apple", "banana", "cherry"), size = 50, replace = TRUE),
                  city = sample(c("heidelberg", "paris", "new york"), size = 50, replace = TRUE),
                  age = rnorm(n = 50, mean = 40, sd = 15))
Y <- matrix(rbinom(n = 4 * 50, mu = 3, size = 1/3.1), nrow = 4, ncol = 50)
fit <- glm_gp(Y, design = ~ fav_food + city + age, col_data = data)
predict(fit)[, 1:3]

nd <- data.frame(fav_food = "banana", city = "paris", age = 29)
predict(fit, newdata = nd)

nd <- data.frame(fav_food = "banana", city = "paris", age = 29:40)
predict(fit, newdata = nd, se.fit = TRUE, type = "response")

```

---

print.glmGamPoi

*Pretty print the result from glm\_gp()*


---

**Description**

Pretty print the result from `glm_gp()`

**Usage**

```
## S3 method for class 'glmGamPoi'
print(x, ...)

## S3 method for class 'glmGamPoi'
format(x, ...)

## S3 method for class 'glmGamPoi'
summary(object, ...)

## S3 method for class 'summary.glmGamPoi'
print(x, ...)

## S3 method for class 'summary.glmGamPoi'
format(x, ...)
```

**Arguments**

x	the glmGamPoi object
...	additional parameters, currently ignored
object	the glmGamPoi object that is summarized

**Value**

The print() methods return the object x. The format() method returns a string. The summary() method returns an object of class summary.glmGamPoi.

---

residuals.glmGamPoi    *Extract Residuals of Gamma Poisson Model*

---

**Description**

Extract Residuals of Gamma Poisson Model

**Usage**

```
## S3 method for class 'glmGamPoi'
residuals(
  object,
  type = c("deviance", "pearson", "randomized_quantile", "working", "response"),
  ...
)
```



**Arguments**

<code>object</code>	a fit of type <code>glmGamPoi</code> . It is usually produced with a call to <code>glm_gp()</code> .
<code>type</code>	the type of residual that is calculated. See details for more information. Default: "deviance".
<code>...</code>	currently ignored.

**Details**

This method can calculate a range of different residuals:

**deviance** The deviance for the Gamma-Poisson model is

$$dev = 2 * (1/theta * \log((1 + m * theta) / (1 + y * theta)) - y \log((m + y * theta) / (y + y * m * theta)))$$

and the residual accordingly is

$$res = \text{sign}(y - m) \sqrt{dev}.$$

**pearson** The Pearson residual is  $res = (y - m) / \sqrt{m + m^2 * theta}$

**randomized\_quantile** The randomized quantile residual was originally developed by Dunn & Smyth, 1995. Please see that publication or `statmod::qresiduals()` for more information.

**working** The working residuals are  $res = (y - m) / m$ .

**response** The response residuals are  $res = y - m$

**Value**

a matrix with the same size as `fit$data`. If `fit$data` contains a `DelayedArray` than the result will be a `DelayedArray` as well.

**See Also**

[glm\\_gp\(\)](#) and `'stats::residuals.glm()`

---

<code>solve_lm_for_A</code>	<i>Solve the equation <math>Y = A B</math> for <math>A</math> or <math>B</math></i>
-----------------------------	---

---

**Description**

Solve the equation  $Y = A B$  for  $A$  or  $B$

**Usage**

```
solve_lm_for_A(Y, B, w = NULL)
```

```
solve_lm_for_B(Y, A, w = NULL)
```

**Arguments**

Y	the left side of the equation
w	a vector with weights. If NULL it is ignored, otherwise it must be of length 1 or have the same length as columns in Y. Default: NULL
A, B	the known matrix on the right side of the equation

---

test\_de

*Test for Differential Expression*


---

**Description**

Conduct a quasi-likelihood ratio test for a Gamma-Poisson fit.

**Usage**

```
test_de(
  fit,
  contrast,
  reduced_design = NULL,
  full_design = fit$model_matrix,
  subset_to = NULL,
  pseudobulk_by = NULL,
  pval_adjust_method = "BH",
  sort_by = NULL,
  decreasing = FALSE,
  n_max = Inf,
  verbose = FALSE
)
```

**Arguments**

fit	object of class glmGamPoi. Usually the result of calling glm_gp(data, ...)
contrast	The contrast to test. Can be a single column name (quoted or as a string) that is removed from the full model matrix of fit. Or a complex contrast comparing two or more columns: e.g. A - B, "A - 3 * B", (A + B) / 2 - C etc. Only one of contrast or reduced_design must be specified.
reduced_design	a specification of the reduced design used as a comparison to see what how much better fit describes the data. Analogous to the design parameter in glm_gp(), it can be either a formula, a model.matrix(), or a vector. Only one of contrast or reduced_design must be specified.
full_design	option to specify an alternative full_design that can differ from fit\$model_matrix. Can be a formula or a matrix. Default: fit\$model_matrix

subset_to	a vector with the same length as <code>ncol(fit\$data)</code> or an expression that evaluates to such a vector. The expression can reference columns from <code>colData(fit\$data)</code> . A typical use case in single cell analysis would be to subset to a specific cell type (e.g. <code>subset_to = cell_type == "T-cells"</code> ). Note that if this argument is set a new the model for the <code>full_design</code> is re-fit. Default: NULL which means that the data is not subset.
pseudobulk_by	a vector with the same length as <code>ncol(fit\$data)</code> that is used to split the columns into different groups (calls <code>split()</code> ). <code>pseudobulk_by</code> can also be an expression that evaluates to a vector. The expression can reference columns from <code>colData(fit\$data)</code> . The counts are summed across the groups to create "pseudobulk" samples. This is typically used in single cell analysis if the cells come from different samples to get a proper estimate of the differences. This is particularly powerful in combination with the <code>subset_to</code> parameter to analyze differences between samples for subgroups of cells. Note that this does a fresh fit for both the full and the reduced design. Default: NULL which means that the data is not aggregated.
pval_adjust_method	one of the p-value adjustment method from <a href="#">p.adjust.methods</a> . Default: "BH".
sort_by	the name of the column or an expression used to sort the result. If <code>sort_by</code> is NULL the table is not sorted. Default: NULL
decreasing	boolean to decide if the result is sorted increasing or decreasing order. Default: FALSE.
n_max	the maximum number of rows to return. Default: Inf which means that all rows are returned
verbose	a boolean that indicates if information about the individual steps are printed while fitting the GLM. Default: FALSE.

## Value

a `data.frame` with the following columns

**name** the rownames of the input data

**pval** the p-values of the quasi-likelihood ratio test

**adj\_pval** the adjusted p-values returned from `p.adjust()`

**f\_statistic** the F-statistic:  $F = (Dev_{full} - Dev_{red}) / (df_1 * disp_{ql} - shrunken)$

**df1** the degrees of freedom of the test: `ncol(design) - ncol(reduced_design)`

**df2** the degrees of freedom of the fit: `ncol(data) - ncol(design) + df_0`

**lfc** the log2-fold change. If the alternative model is specified by `reduced_design` will be NA.

## References

- Lund, S. P., Nettleton, D., McCarthy, D. J., & Smyth, G. K. (2012). Detecting differential expression in RNA-sequence data using quasi-likelihood with shrunken dispersion estimates. *Statistical Applications in Genetics and Molecular Biology*, 11(5). <https://doi.org/10.1515/1544-6115.1826>.

**See Also**

[glm\\_gp\(\)](#)

**Examples**

```

Y <- matrix(rnbinom(n = 30 * 100, mu = 4, size = 0.3), nrow = 30, ncol = 100)
annot <- data.frame(sample = sample(LETTERS[1:6], size = 100, replace = TRUE),
                    cont1 = rnorm(100), cont2 = rnorm(100, mean = 30))
annot$condition <- ifelse(annot$sample %in% c("A", "B", "C"), "ctrl", "treated")
head(annot)
se <- SummarizedExperiment::SummarizedExperiment(Y, colData = annot)
fit <- glm_gp(se, design = ~ condition + cont1 + cont2)

# Test with reduced design
res <- test_de(fit, reduced_design = ~ condition + cont1)
head(res)

# Test with contrast argument, the results are identical
res2 <- test_de(fit, contrast = cont2)
head(res2)

# The column names of fit$Beta are valid variables in the contrast argument
colnames(fit$Beta)

# You can also have more complex contrasts:
# the following compares cont1 vs cont2:
test_de(fit, cont1 - cont2, n_max = 4)

# You can also sort the output
test_de(fit, cont1 - cont2, n_max = 4,
        sort_by = "pval")

test_de(fit, cont1 - cont2, n_max = 4,
        sort_by = - abs(f_statistic))

# If the data has multiple samples, it is a good
# idea to aggregate the cell counts by samples.
# This is called "pseudobulk".
test_de(fit, contrast = "conditiontreated", n_max = 4,
        pseudobulk_by = sample)

# You can also do the pseudobulk only on a subset of cells:
cell_types <- sample(c("Tcell", "Bcell", "Makrophages"), size = 100, replace = TRUE)
test_de(fit, contrast = "conditiontreated", n_max = 4,
        pseudobulk_by = sample,
        subset_to = cell_types == "Bcell")

# Be care full, if you included the cell type information in

```

```
# the original fit, after subsetting the design matrix would
# be degenerate. To fix this, specify the full_design in 'test_de()'
SummarizedExperiment::colData(se)$ct <- cell_types
fit_with_celltype <- glm_gp(se, design = ~ condition + cont1 + cont2 + ct)
test_de(fit_with_celltype, contrast = cont1, n_max = 4,
        full_design = ~ condition + cont1 + cont2,
        pseudobulk_by = sample,
        subset_to = ct == "Bcell")
```

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